

# Unsupervised Retinal Blood Vessel Segmentation Technique using *pdAPSO* and Difference Image Methods for Detection of Diabetic Retinopathy

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**Abstract**—Retinal vessel segmentation is a practice that has the potential of enhancing accuracy in the diagnosis and timely prevention of illnesses that are related to blood vessels. Acute damage to the retinal vessel has been identified to be the main cause of blindness and impaired vision. A timely detection and control of these illnesses can greatly decrease the number of loss of sight cases. However, the manual protocol for such detection is laborious and although autonomous methods have been recommended, the accuracy of these methods is often unreliable. We propose the utilization of the Primal-Dual Asynchronous Particle Swarm Optimisation (*pdAPSO*) and differential image methods in addressing the drawbacks associated with segmentation of retinal vessels in this study. The fusion of *pdAPSO* and differential image (which focuses on the median filter) produced a significant enhancement in the segmentation of huge and miniscule retinal vessels. In addition, the method also decreased erroneous detection near the edge of the retinal (that is not sensitive to light). The results are favourable for the median filter when compared to mean filter and Gaussian filter. The accuracy rate of 0.9559 (with a specificity of sensitivity rate of 0.9855), and a sensitivity rate of 0.7218 were obtained when tested using the Digital Retinal Images for Vessel Extraction database. The above result is a pointer that our approach will help in detecting and diagnosing the damage done to the retinal and thereby preventing loss of sight.

**Keywords/Index Terms**—Retinal Vessel, Segmentation, Asynchronous Particle Swarm Optimisation, Primal-Dual, Diabetic Retinopathy

## 1. Introduction

Retinopathy is the subdivision of medicine that makes it possible to determine the cause of infections and ailments of the eye and treat them immediately. Digital photography and image analysis of retinal vessel are already gaining ground. The studies of (Kanski, 2007) and (Klonoff & Schwartz, 2000) observed that these techniques have been recently recognised as beneficial techniques in the identification and treatment of some diseases like diabetic retinopathy (DR), retinopathy of prematurity (ROP) which is a pathological disarrange of the retina and cardiovascular diseases (Mapayi, Tapamo & Viriri, 2014).

According to World Health Organisation (2016), DR and ROP are the chief reasons of eye defect and impaired vision universally, timely identification of the cause and control of these ailments will assist in a notable decrease of instances of impaired vision (Gergely & Gerinec, 2009). Ophthalmologists find vessel network very useful as they concentrate on retinal vessel quality assessment at some stage of diseases diagnosis. Detection by physical examination and testing of the retinal vessels in the hollow part of the images is quite cumbersome and laborious job which needs competent and skillful people who are not readily available (Varughese, *et al.*, 2008). Nevertheless, according to Marrugo *et al.*, (2012), it is possible for the ophthalmologist to diagnose and effectively control the diseases with the help of automated segmentation and systematic inspection of the arrangement of blood vessels in the retinal. Retinal vessel segmentation is the partitioning of a retinal image into

sections that have related attributes such as grey level, colour, texture, brightness, and contrast (Zhang, Zhou & Bao, 2015). The image part is removed from the initial image during image analysis and image segmentation algorithms are used to divide the original image into different segments. The main purpose of the retinal vessel segmentation is to divide the retinal image into equally exclusive sections so that each section in relation to the pixel concentration is harmonised to a predetermined benchmark (Zhang, Zhou & Bao, 2015). This study presents a new technique for segmenting network vessels in retinal images through Difference image and *pdAPSO* techniques.

The remainder of this paper is structured as follows: Section 2 discusses the related works. Section 3 discusses our proposed methodology, filtering techniques, difference image, primal-dual particle swarm optimisation and post-processing. The results generated by our proposed approach on DRIVE datasets and discussions are specified in Section 4, and lastly the study is concluded in Section 5.

## 2. Related Works

Many research has been conducted in the area of retinal segmentation. Akram & Khan (2013) used a multi-layered thresholding-based blood vessel segmentation method for investigating cases of retinal diabetic that can result in blindness. Jiang & Mojon (2003) used an adaptive local thresholding prototype employing an authentication based multi-threshold analytical system for detecting the retinal image. The weakness of this approach is its lackluster performance in detecting the reedier vessels and some isolated vessels in the retinal. Mapayi, Viriri &

Tapamo (2015) proposed a novel adaptive thresholding method for retinal vessel segmentation using local information that is uniform in nature. Qin *et al.*, (2006) employed a multiscale method that uses Gabor filters and scale multiplication for the segmentation of retinal vessels. Marin *et al.*, (2011) developed a novel supervised approach for blood vessel segmentation in retinal images through gray-level and moment invariants-based features for pixel depiction, whereas the vessel segmentation was done by neural network algorithm. Szpak & Tapamo (2008) used the gradient based technique and level set method for retinal vessels segmentation. Their approach was unsuccessful in detecting the tinnier retinal vessels. Wang *et al.*, (2013) used the combination of multi-wavelet kernels and multiscale hierarchical decomposition to segment retinal vessels. Xiao *et al.*, (2013) developed a retinal segmentation technique based on the Bayesian method and spatial constraint. Yin *et al.*, (2013) proposed an unsupervised segmentation technique using probabilistic formulation.

Lupascu & Tegolo (2011) implemented an unsupervised segmentation of retinal vessels using self-organizing maps (SOM) and k-means clustering. The SOM is trained on retinal images and the map was again partitioned by k-means clustering method into two groups. The complete image is again passed to SOM and the group with the most ideal identical section on SOM is allocated to each pixel. A hill climbing scheme on associated components is employed to detect the vessel network during the post-processing operation.

Ramaswamy *et al.*, (2011) proposed the combination of k-means and fuzzy c-means clustering methods for the categorisation of discharges and non-discharges in retinal images. Saffarzadeh *et al.*, (2014) developed a technique that used k-mean for pre-processing after which the multi-scale line operator is utilised for the detection of retinal vessel network. The K-means assists the vessels to be more conspicuous and there is a significant decrease in the effect of bright gashes. The line detection operator in three scales is used in detecting the retinal vessels. Wen *et al.*, (2007) assessed the performance of the k-means algorithm in enhancing the detection of retinal vessels by decreasing the colour space. However, the output of this approach was not good.

Sreejini & Govindan (2015) applied PSO to find the best filter parameters of the multiscale Gaussian matched filter to attain increased accuracy of retinal vessel segmentation. Their technique have better performance than many of the existing retinal vessel segmentation methods. There is still need to improve on the performance of the proposed system as the mutiscale matched filter does not completely overcome the problem of undesirable performance figures of matched filters. Son, Park & Jung (2017) used generative adversarial neural network to produce the exact map of retinal vessels on DRIVE and STARE datasets. The drawback of their approach is that it was unsuccessful in detecting extremely tinny vessels. Li *et al.*, (2017) applied reinforcement local descriptions and SVM to segment retinal blood vessel. The system achieved a very high performance but

the segmentation process can be time consuming. Mohsen *et al.*, (2018) proposed neural network hardware implementation and FPGA for retinal vessel segmentation. The major drawback of their technique is the complexity of the system. Memari *et al.*, (2017) used the hybrid of matched filter and AdaBoost classifier for enhanced retinal vessel segmentation. Sumathi, Vivekanandan & Ravikanth (2018) proposed neural network for efficiently segmenting retinal vessel.

Particle swarm optimisation (PSO) algorithm is an unsupervised segmentation approach. PSO has found application in the field of image segmentation. Saatchi & Cheng-Hung (2007) did a survey of image segmentation application of swarm intelligence algorithms (PSO and ACO) and their hybrid with k-means and simple competitive learning algorithms. Gopi & Nageswara (2013) used PSO methods for image segmentation to detect breast cancer. Their experimental result shows that the fusion of Fuzzy C-means (FCM) and Fractional Order Darwinian PSO (FODPSO) algorithm performs better than the PSO alone, and Darwinian PSO (DPSO). There is, however, need to develop the more efficient approach that can remove background noise from the images. Mahalakshmi & Velmurugan (2015) used PSO to segment a brain tumour medical images. The effectiveness of the approach is not certain as there is no clear parameter for measuring the performance of the technique.

While much progress has been made in developing efficient methods by the earlier research works, the results

indicates that there is need for more work to be done in tackling the problem of high false detection close to the edge of the point where the optic nerve enters the retinal and the segmentation of big and reedier retinal vessels. In this study, we propose the combination of the Primal-Dual Asynchronous particle swarm optimisation and difference image approach for the segmentation of retinal blood vessel segmentation for easy detecting of thinner layers in the vessel and effective diagnosis of retinopathy diabetics. The major shortcoming of many of the vessel segmentation techniques include: low contrast of vessels, low quality images and large disparities and unpredictability in the size of the vessels. Achieving high accuracy in segmentation is a big problem because minute vessels are subjugated by various image noises such as Gaussian (Sreejini & Govindan, 2015).

### 3. Methodology

Normally, the presence of noise as a result of fluctuating lighting and contrast in retinal fundus images pose a challenge to retinal image clustering unless there is pre-processing operation. Realising the fact that efficient detection of the network of the vessel is a crucial phase required in the detection of diseases of the eye for dependable retinal vessel classification, there is need to develop an effective method that can handle the segmentation of sizable and small vessels in a well-timed and successful style. The green section of the pigmented retinal image is utilised for segmentation because it offers the most excellent brightness setting for the vessel (Kande, Subbaiah & Savithri, 2010). An in-depth explanation of our

proposed technique is outlined below:

- (1) Removal of the green channels of the coloured retina image.
- (2) Filtering of the retinal image using median, mean, and Gaussian filtering methods.
- (3) Producing the difference image.
- (4) Partitioning of the retinal vessels

from the difference image produced by the *pdAPSO* algorithm.

- (5) Execution of a post-processing stage using median filter for the elimination of miscategorisation.

Figure 1 below depicts the framework of the proposed system.

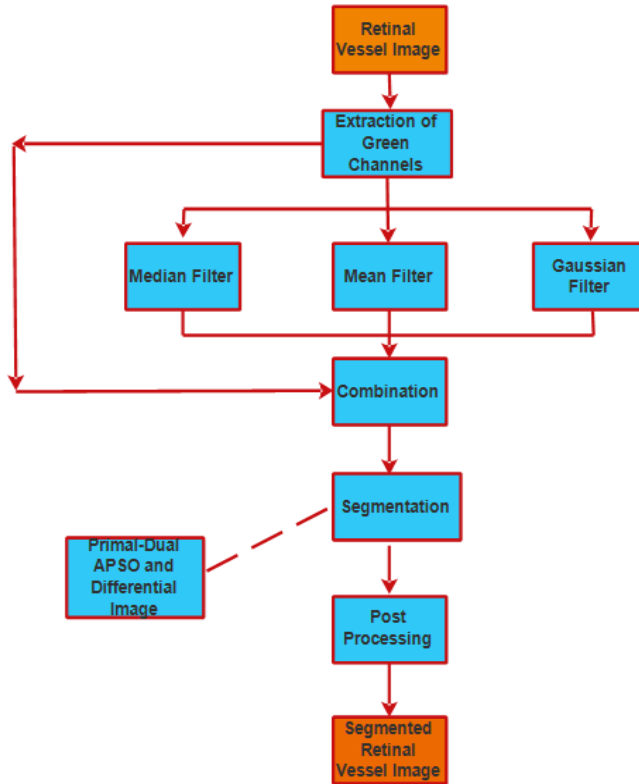


Figure 1: Framework of the proposed technique (the technique comprises of basically three steps using different filters and combinations of filters and a segmentation technique).

### 3.1 Filtering Techniques

The improvement of the green channel of the fundus retinal image is by achieved applying diverse filtering methods. The mean filter and Gaussian filter which are linear filters are employed to free the images from roughness and unevenness of the surface. These filters help to decrease image noise. However, they cannot

effectively protect the boundaries of an image. The median filter which is a non-linear filter is very effective in eliminating image noise in addition to safeguarding information at the borderline of images. It is very essential for us to state that the dimensions of the frame of the chosen image should not be too big to be able to proficiently handle the noise resulting from brightness

deviation that usually characterises the retinal image. Being meticulous in the choice of window size that has adequate data points is very crucial to achieving for good enhancement. Choosing window sizes with adequate data points is crucial to attaining superior enhancement in the segmentation process. In this study, we employ the mean, Gaussian and median filters because of the complexity of the retinal image. The complexity of the retinal image is explained below:

$$R = F \otimes G \tag{1}$$

$$R_{(i,j)} = \sum_{(x,y) \in F} \sum_{(i-x,j-y) \in G} F(x,y) G(i-x,j-y) \tag{2}$$

Given that R is the twisted retinal image, G represents the green channel of the retinal image and the twisted cover F is used to denote the filtering method used in this research work

### 3.2 Difference Image

The subtraction of the green channel of the coloured retinal image from the twisted retinal image produced the difference image. The formula for the difference image D(i, j) is as follows:

$$D(i,j) = R(i,j) - G [i,j] \tag{3}$$

where  $D(i,j) = \{D_q(i,j), D_G(i,j), D_\alpha(i,j)\}$ , here  $D_q(i,j)$  is the difference image created by median filter (DIMDF),  $D_G(i,j)$  is the difference image created by mean filter (DIMNF) and  $D_\alpha(i,j)$  is the difference image created by Gaussian filter (DIGF). We also experimented with using the combination of median and mean filters (DIMDMNF), median and Gaussian filters (DIMDGF), and mean and trajectory of the  $i^{th}$  particle. Consequently, a swarm typifies a number of contending cluster centers.

Gaussian filters (DIMNGF). The possible permutations are

$$D_q^G = D_G(i,j) + D_q(i,j)$$

$$D_G^q = D_q(i,j) + D_G(i,j) \tag{5}$$

$$D_\alpha^G = D_\alpha(i,j) + D_G(i,j) \tag{6}$$

where  $D_q^G$  represents the DIMDMNF, and  $D_G^q$  is used to denote the DIMDGF, while  $D_\alpha^G$  represents the DIMNGF. The outputs of the equations (4) to (6) are regularised to the interval [0, 255].

### 3.3 Primal-Dual Asynchronous Particle Swarm Optimisation (pdAPSO) Algorithm

The Asynchronous PSO (APSO) is a variant of PSO proposed by Dada and Effirul (2015). The current personal best ( $pbest_{i,m}$ ) and the global best ( $gbest_{i,m}$ ) of a particle, its velocities, and positions of particles are instantly modified to be up to date after computing their fitness. As a result of this, the parameters are updated using partial or deficient information about the neighbourhood. This leads to diversities in the swarm of particles as the current swarm is a mixture of certain information from the earlier iteration and the ones from the current iteration. For detail information on the Primal-Dual PSO, the reader is referred to our previous work (Dada & Effirul, 2015). This present study adapted the *pdAPSO* algorithm for efficient segmentation of retinal images. In this approach, a single particle  $x_i$  denotes N cluster such that  $x_i = (y_{i1}, \dots, y_{ij}, \dots, y_{iN})$  where  $y_{ij}$  correspond to the  $j^{th}$  cluster centre of inertia. The fitness of each group of cluster is computed based on the formula below:

$$f(x_i, m_i) = w_1 \text{dist}_{\max}(m_i, x_i) + w_2 (m_{\max} -$$

$dist_{\min}(x_i)$  (7)  
 where  $Z_{\max} = 2n-1$  for an n-bit image; M is a matrix denoting the allocation of pixels to clusters of particle i. Each element  $m_{ijp}$  specifies if the pixel  $m_p$  is a member of cluster  $C_{ij}$  of particle i. The coefficients  $w_1$  and  $w_2$  are constants that are specified by the user. Similarly, the highest value of the mean Euclidean distance of particles to their related clusters is

$$dist_{\max}(m_i, x_i) = \max_{j=1, \dots, N_e} \{ \sum_{\forall m_p \in C_i} dist(m_p, y_{ij}) / |c_{ij}| \} \quad (8)$$

and the distance between any set of clusters with the lowest Euclidean distance value is  $dist_{\min}(x_i) = \min_{\forall j_1, j_2, j_1 \neq j_2} \{ d(y_{ij_1}, y_{ij_2}) \}$  (9)

The flowchart of the *pdAPSO* algorithm is shown in figure 1 below.

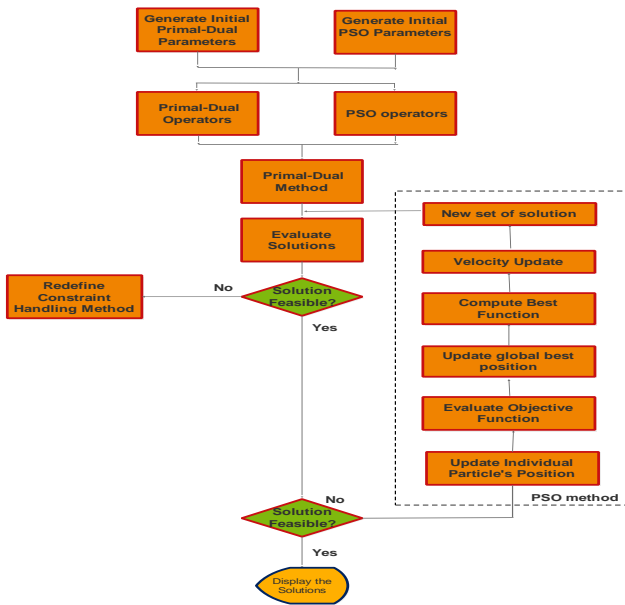


Figure 2: Primal- Dual-APSO (*Pdaps*) Flowchart

The proposed algorithm for retinal vessel segmentation is outlined below:

**Algorithm 1 *pdAPSO* Segmentation algorithm**

Step 1: Haphazardly assign an initial value to cluster centers for each particle.

Step 2: On behalf of each particle, designate each pixel to a cluster with the shortest distance to its cluster center.

Step 3: Compute the fitness function for each particle and obtain the global best solution.

Step 4: Save the best solution found so far as the *pbest* or personal best solution.

Step 5: Use the equations below to update the cluster centers

$$v_{i,m}^{(t+1)} = w * v_{i,m}^{(t)} + c_1 * rand() * (pbest_{i,m} - x_{i,m}^{(t)}) + c_2 * rand() * (gbest_m - x_{i,m}^{(t)}) \quad (10)$$

$$x_{i,m}^{(t+1)} = x_{i,m}^{(t)} + v_{i,m}^{(t+1)} \quad (11)$$

Step 6: If the stopping condition is fulfilled move to the subsequent step. Else, move to Step 3.

Step 7: Display the best solution.

The Primal-Dual Asynchronous Particle Swarm Optimisation method explained in Algorithm 1 is utilised in segmenting the retinal vessel network from the contextual tissue in the retinal images by utilising the outputs produced of equations (10) and (11).

### 3.4 Post-Processing

Median filter is utilised for the post-processing stage to ensure the reduction to the barest minimum of erroneously detected pixels in the vessel. We adopted a 2×2 median filter to remove the noisy pixels in the image to so that we can get the segmented vessel network. The median filter works by taking into consideration each pixel in the vessel image in turn and considers at its close neighbours to determine if it is a true exemplification of its surroundings. Rather than just merely changing the pixel values, it substitutes it with the median of these values. A 2x2 neighbourhood is considered here as larger neighbourhoods will produce better smoothing in the retinal vessel image. The median filter is very robust and it does not generate fresh impracticable pixel values when the filter overlaps a border. This makes it to be much better at maintaining sharp edges than some other filters.

### 3.5 Performance Measures

In this section, the experimental setup used to evaluate three algorithms proposed for retinal vessel segmentation. The sensitivity, specificity, and accuracy are the main performance metrics used in this work. The algorithms were experimented on the DRIVE database explained in section 3.3.

$$\text{Sensitivity} = TP / (TP + FN) \quad (12)$$

$$\text{Specificity} = TN / (TN + FP) \quad (13)$$

$$\text{Accuracy} = (TP + TN) / (TP + TN + FP + FN) \quad (14)$$

where TP = True Positive, TN = True Negative, FP = False Positive and FN = False Negative.

The amount of pixels that are rightly categorised as vessel pixels is the TP. The amount of pixels that are rightly categorised as non-vessel pixels is the TN, while FN is the number of pixels wrongly categorised as non-vessel pixels. The FP is the number of pixels wrongly categorised as vessel pixels. The sensitivity (SE) is the division of TP by the sum of vessel pixels in the ground truth segmentation, while the specificity (SP) is the division of TN by the sum of non-vessel pixels in the ground truth.

## 4. Results and Discussion

Some tests were carried out to ascertain the efficiency of our new technique. Our technique was tested using DRIVE database on <http://www.isi.uu.nl/Research/Databases/DRIVE>. Experiments were conducted using MATLAB 2015a on an AMD A 10-7300 Radeon R6, 10 Compute Cores 4C+6G, 1.90 GHz, 8.00GB of RAM. The optimal parameters for the filtering operation were discovered by inputting one of the images into the optimised median filter. The *pdAPSO* optimisation technique comprises of diverse arbitrary processes. It therefore means that using identical parameters for the filter does not guarantee getting the same result even when the program is restarted and executed.

### 4.1 Results

The results of our experiments indicate the performance of the diverse difference images hybridised with the *pdAPSO* algorithm. *pdAPSO* and



DIMDF produced the most ideal segmentation result when compared to *pdAPSO* and DIMNF then *pdAPSO* and DIGF. *pdAPSO* and DIMDF generated the most superior accuracy rate 0.9559 and a specificity rate of 0.9855. In Figure 3, we provide a pictorial explanation that relates the results gotten from vessels segmented by *pdAPSO* and difference image using each of the filters.

#### 4.2 Discussion

The fusion of DIMDF and *pdAPSO* detected many of the big and tinny vessels, whereas some few gauzier vessels go on without detection. There are few cases of erroneous detection coupled with previous leftover close to the edge of the point where the optic nerve enters the retinal. The erroneous detection near the edge of the optic disc is nevertheless greatly reduced on the segmented vessels by DIMDF and *pdAPSO* but much in number on segmented vessels generated by the combination of *pdAPSO* with DIMNF, and *pdAPSO* with DIGF. The reason for this is because the median filter maintains boundary information of the vessels in the improved retinal image. Furthermore, the DIMDMNF and DIMDGF while hybridised with *pdAPSO* produced good sensitivity of 0.7217 and 0.7205 respectively. The addition of DIMDF caused the increase in sensitivity of the retinal image. However, the accuracy of DIMDF is

better than the ones generated by DIMDMNF, DIMDGF, and DIMNGF while fused with the *pdAPSO* method. The statistical results generated by our approach are presented in table 1.

In Fig. 4 there is a visual description of the result comparison of retina vessels segmented by the fusion of *pdAPSO* and DIMDF DIMDMNF, DIMDGF and DIMNGF. As illustrated in Fig. 3, a good number of the large and tinny vessels are detected, while the ones that remain undetected are very few. The erroneous detection near the edge of the optic nerve is greater on the outputs generated by DIMDMNF, DIMDGF and DIMNGF while fused with *pdAPSO* but smaller on the outputs produced through *pdAPSO* fused with DIMDF. This explains the reason why a better accuracy rate was attained.

#### 4.3 Performance comparison of *pdAPSO* with other segmentation techniques on DRIVE dataset

The performance comparison of some of the segmentation techniques on DRIVE database is presented in Table 2. The combinations of the proposed approach with the best performance yield higher and specificity rates, when compared to the earlier approaches. It is worth noting that the work of Ricci & Perfetti (2007) generated the highest accuracy rate among all the techniques compared, the value for the sensitivity and specificity rates are not specified.

Table 1: Performances of Selected Segmentation Techniques on Drive

Technique	Accuracy	Sensitivity	Specificity
<i>pdAPSO</i> and DIMDF	0.9559	0.7218	0.9855
<i>pdAPSO</i> and DIMNF	0.9551	0.7092	0.9824
<i>pdAPSO</i> and DIGF	0.9552	0.7056	0.9869
<i>pdAPSO</i> and IMDMNF	0.9545	0.7217	0.9703
<i>pdAPSO</i> and DIMDGF	0.9542	0.7205	0.9726
<i>pdAPSO</i> and DIMNGF	0.9505	0.7108	0.9759

Table 2: Performances of Selected Segmentation Techniques on Drive

Technique	Accuracy	Sensitivity	Specificity
Human observer	0.9473	0.7761	0.9725
Mapayi <i>et al.</i> , (2015)	0.9469	0.7477	0.9680
Saffarzadeh <i>et al.</i> , (2014)	0.9387	N/A	N/A
Xiao <i>et al.</i> , (2013)	0.9529	0.7513	0.9792
Oliveira <i>et al.</i> (2016)	0.9464	N/A	N/A
Meng <i>et al.</i> (2016)	0.9630	0.7680	0.9827
Mohsen <i>et al.</i> (2017)	0.9469	0.5147	0.9950
Memari <i>et al.</i> (2017)	0.9321	0.8124	0.9505
Sumathi, Vivekanandan & Ravikanth (2018)	0.9671	0.8139	0.9822
Proposed Technique	0.9559	0.7218	0.9855

The result below shows the images produced by the fusion of difference image and *pdAPSO* algorithm.

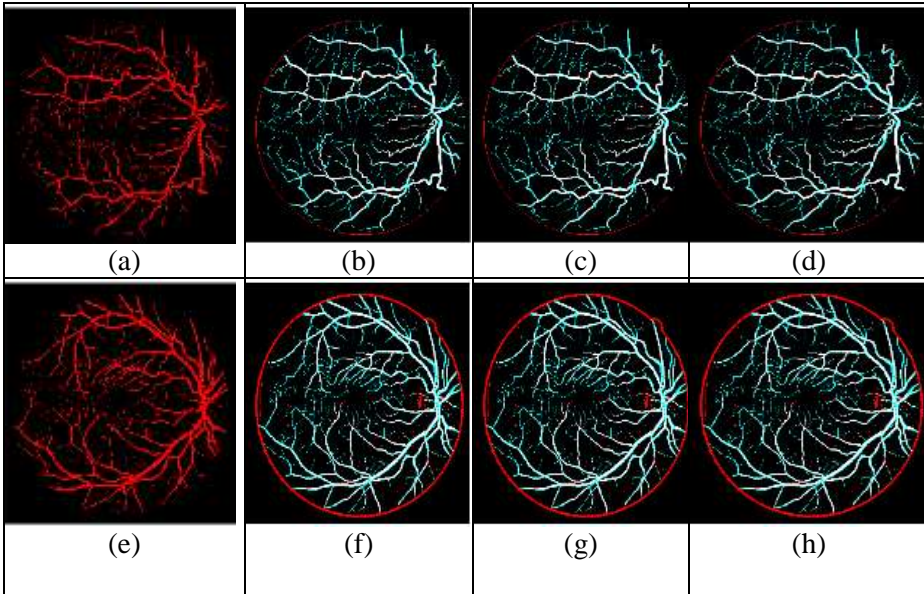


Fig. 3: (a) & (e) DRIVE Database Gold Standard. (b) & (f) Segmented Vessels Using *pdAPSO* and DIMDF. (c) & (g) Segmented Vessels Using *pdAPSO* and DIMNF. (d) & (h) Segmented Vessels Using *pdAPSO* and DIGF.

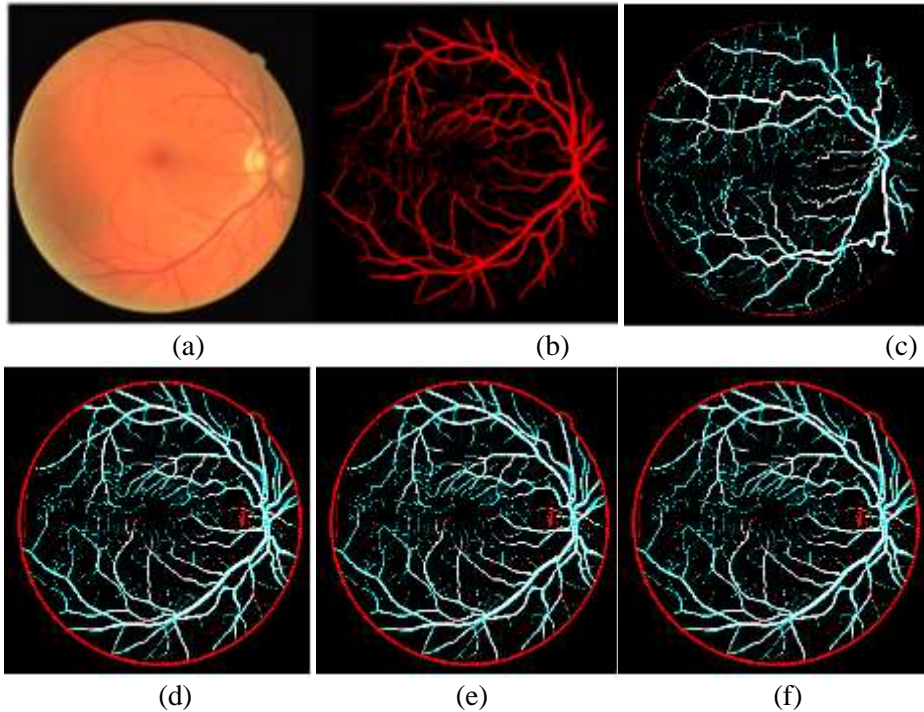


Fig. 4: (a) DRIVE Database Coloured Fundus Image (b) DRIVE Database Gold Standard (c) Segmented Vessels Using *pdAPSO* and DIMDF (d) Segmented Vessels Using *pdAPSO* and DIMNGF (e) Segmented Vessels Using *pdAPSO* and DIMDGF (f) Segmented Vessels Using *pdAPSO* and DIMDMNF

## 5. Conclusion

In this study, the hybrid of difference image and *pdAPSO* was used for the segmenting the retinal vessels. It was demonstrated that the proposed vessel segmentation technique is time efficient and yields a high accuracy, specificity rates, and sensitivity when compared to some segmentation methods on DRIVE database. The fusion of *pdAPSO* and difference image centered on median filter effectively segmented both large and tinny retinal vessels and also reduced erroneous detection near the edges of the optic disc. The results also proved the superiority of the hybrid of *pdAPSO* and difference image centered on median filter compared to difference image centered on mean filter and difference image centered on Gaussian filter fused with *pdAPSO* for the segmentation of retinal vessels. Moreover, the capacity of the median filter to preserve the boundaries of the

retinal image is the reason for the outstanding performance. This work also proved that the hybridisation of *pdAPSO* with difference images centered on linear filtering technique and difference image centered on the median filter generated an excellent vessel segmentation result. Finally, we deduced from our experiments that our proposed method that integrates difference image with *pdAPSO* produced accuracy, specificity and sensitivity that are as good as that of other earlier methods on DRIVE database. Future work, will concentrate on developing more effective segmentation methods using Softcomputing algorithms such as Moth flame Optimisation and Grey Wolf Optimisation algorithms, and also exploit filters such as Gabor Wavelet filters, matched filter, and Frangi's filters.

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